

Calculus Warm Up # 7- 4

Test day, no warm up.

Turn it in.

Back into Chapter 7 starting Monday.

Exponential and Logarithmic Functions

7.2 Integration of Exponential Functions

## Integration Rules

Let  $u$  be a differentiable function of  $x$ .

$$1. \int e^x dx = e^x + C \quad 2. \int e^u du = e^u + C$$

$$\begin{aligned} & \int e^{3x+1} dx && \text{Let } u = 3x+1 \\ & && du = 3 dx \\ &= \frac{1}{3} \int 3e^{3x+1} dx \\ &= \frac{1}{3} \int e^u du \rightarrow = \boxed{\frac{1}{3} e^{3x+1} + C} \end{aligned}$$

Evaluate:

$$1. \int 5xe^{-x^2} dx \quad \begin{array}{l} u = -x^2 \\ du = -2x dx \end{array}$$

$$= -\frac{5}{2} \int -2x e^{-x^2} dx$$

$$= -\frac{5}{2} \int e^u du$$

$$= \boxed{-\frac{5}{2} e^{-x^2} + C}$$

$$2. \int \frac{e^{1/x}}{x^2} dx$$

$$\begin{array}{l} u = \frac{1}{x} \\ du = -\frac{1}{x^2} dx \end{array}$$

$$= - \int e^u du$$

$$= \boxed{-e^{1/x} + C}$$

3.  $\int (1 + e^x)^2 dx$  Rewrite:

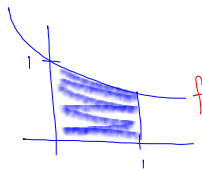
$$= \int (1 + 2e^x + e^{2x}) dx$$

$$= \int 1 dx + 2 \int e^x dx + \frac{1}{2} \int 2e^{2x} dx$$

$$= x + 2e^x + \frac{1}{2}e^{2x} + C$$

4. Find the area of the region bounded by

$f(x) = e^{-x}$  and the x-axis on  $[0, 1]$ .



$$A = - \int_0^1 e^{-x} dx \quad \begin{matrix} u = -x \\ du = -dx \end{matrix}$$

$$= - \left[ e^{-x} \right]_0^1$$

$$= - \left( \frac{1}{e} - e^0 \right)$$

$$= \boxed{-\frac{1}{e} + 1}$$

HW: From 7.2,

Read: p. 366 - 369,

Do: p. 370 # 43 - 69 odd